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Accepted: 04 August 23

Posted: 09 August 23

DOI: https://doi.org/10.1364/OL.496312
Nonlinear distortion mitigation of DML-based OFDM optical systems with non-orthogonal DFT-precoding

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Received XX Month XXXX; revised XX Month, XXXX; accepted XX Month XXXX; posted XX Month XXXX (Doc. ID XXXXX); published XX Month XXXX

We propose a non-orthogonal DFT-matrix precoding scheme for the mitigation of the nonlinear distortion induced by the interaction between laser chirp and fiber dispersion in a directly modulated laser (DML)-based orthogonal frequency division multiplexing (OFDM) transmission system. Compared with the conventional OFDM, the proposed method can decrease the peak-to-average power ratio and significantly reduce the nonlinear distortion without sacrificing spectral efficiency. The cascaded binary-phase-shift-keying iterative detection algorithm is used to eliminate the inter-carrier interference that is purposely induced by the non-orthogonal precoding. The performance of the proposed scheme is experimentally evaluated, achieving ~0.4-dB sensitivity improvement at the KP4-forward error correction threshold over the T/2-spaced third-order Volterra nonlinear equalizer (VNLE). Meanwhile, compared to the VNLE, the reduction in computational complexity of one OFDM frame is 90% for multiplication and 88.32% for addition, respectively, in this work. © 2023 Optica Publishing Group

http://dx.doi.org/10.1364/OL.XXXXXX

The intensity modulation and direct detection (IM/DD) optical system has been extensively studied due to its low cost and complexity [1–3]. To further reduce the cost and complexity, directly modulated laser (DML) is preferred over the schemes using additional external modulators, such as electro-absorption modulators and Mach-Zehnder modulators (MZM) [4, 5]. With the merits of flexible modulation and high resilience to fiber chromatic dispersion (CD), the orthogonal frequency division multiplexing (OFDM) technique has recently attracted considerable attention and has been applied to DML-based optical communication systems for practical applications [6–8]. However, DML suffers from strong frequency chirp, which induces severe nonlinear distortion when interacting with the CD. Previous approaches to nonlinear distortion mitigation include the subcarrier-to-subcarrier intermixing interference (SSI) cancellation [9] and the Volterra nonlinear equalizers (VNLE) [10]. However, they have either limited performance or high complexity. A gapped-OFDM technique [11] leveraging a frequency gap between the direct current (DC) component and the transmitted subcarriers was proposed to avoid much of the in-band nonlinear distortion, enhancing the signal-to-noise ratio (SNR) performance in the high-frequency band. Nonetheless, it leads to a loss of spectral efficiency (SE) due to the forbidden subcarriers. Though the bit loading (BL) algorithm applied to the rest of the subcarriers can improve SE [11], it inevitably causes high complexity and round-trip delay.

In this Letter, we extend our previous work [12] to employ the gapped-OFDM technique, where the BL is replaced with the recently proposed non-orthogonal discrete Fourier transform precoding (NODFT-p) [13]. Different from the scheme in [13], the pre-coded subcarriers are allocated in the high-frequency band to generate the required frequency gap. In addition to reducing the in-band nonlinear distortion, it does not sacrifice the SE and can decrease the peak-to-average power ratio (PAPR) compared with the conventional OFDM signal. With this proposed method, we have experimentally demonstrated 9.5-Gb/s QAM-4 optical signal transmission over a 100-km standard single-mode fiber (SSMF) using a DML. The results show that the proposed NODFT-p gapped-OFDM signal achieves ~0.4-dB sensitivity improvement at the KP4-forward error correction (FEC) threshold over the T/2-spaced recursive least square (RLS)-based third-order Volterra nonlinear equalizer (VNLE). Meanwhile, compared to the VNLE in this work, the computation complexity reduction of one OFDM frame is 90% for multiplication and 88.32% for addition, respectively.

Fig. 1(a) shows the SNR profile of the conventional OFDM signal...
(230/512) after 100-km SMF transmission under different bias currents. It can be found that the SNR distribution varied with the bias current. Specifically, the SNR of subcarriers close to the DC component (subcarrier index ≤ 50) decreased as the bias current increased, while the SNR of high-frequency subcarriers (subcarrier index ≥ 50) was just the opposite. This is because the transient chirp exhibits a low-pass-filter-like frequency response whereas the adiabatic chirp shows a band-pass-filter-like response when considering the effect of CD [14]. Besides, bias current increasing can enhance adiabatic chirp while suppressing the transient chirp, thus leading to the above observations. Except for this, the relaxation oscillation frequency which increases with the bias current also causes the improvement in high-frequency SNR [6]. Since the nonlinear distortion induced by the interaction between laser chirp and fiber dispersion is mainly distributed in the low-frequency band, discarding the subcarriers near DC can help improve the overall performance, but at the expense of SE [11].

Fig. 1(b) illustrates the principle of the proposed NODFT-p gapped-OFDM to eliminate the nonlinear distortion distributed near the DC component and keep the SE unchanged. It should be noted that the gap structure can only work effectively when bias current ≥ 60 mA since the SNR of high frequency is good enough for transmission and is larger than that of low frequency under this case based on Fig. 1(a). Assuming that the number of subcarriers utilized by the conventional OFDM is \( N \), for the conventional gapped-OFDM, only \( M \) subcarriers \( \{a_{0,6b}, a_{0,6b+1}, \ldots, a_{0,6b} \} \) carry the symbols [11], leaving the \( (N-M) \) subcarriers \( \{a_{0,4}, a_{0,5}, \ldots, a_{0,511} \} \) near the DC component as the gap width, where the low-frequency subcarriers are corresponding to the two edges of the inverse discrete Fourier transform (IDFT) in Fig 1(b) [15]. However, for the proposed NODFT-p gapped-OFDM, the \( M \) subcarriers \( \{a_{0,6b}, a_{0,6b+1}, \ldots, a_{0,6b} \} \) are compressed from the \( N \) subcarriers \( \{S_0, S_1, \ldots, S_{511} \} \) by an \( M \times N (M \leq N) \) NODFT matrix \( W \) to keep the SE unchanged, where its \((m, n)\)-th entry is denoted by \( W_{mn}=\exp(-j2\pi mn/N)/\sqrt{M} \), for \( m=0, 1, \ldots, (M-1) \), and \( n=0, 1, \ldots, (N-1) \). Note that \( W \) is equivalent to the standard DFT matrix when \( M=N \). Considering the mitigation of nonlinear distortion and the increase in SNR of residual subcarriers using the gap structure and the inter-carrier interference (ICI) induced by the non-orthogonal preceding and decoding [13], the value of \( M \) must be optimized to get the best transmission performance given one preset bias current. An inverse NODFT (INODFT) matrix \( W^H \) is employed for decoding at the receiver side, which is the Hermitian transpose of \( W \).

A high peak-to-average-power ratio (PAPR) limits the transmitter power efficiency, which is a crucial problem in an OFDM system. Fig. 2(a) shows the complementary cumulative distribution function (CCDF) of the PAPR curves for different signals, indicating the significantly reduced PAPR provided by the proposed NODFT-p gapped-OFDM signal \((N=M=12)\) when compared with the conventional OFDM case and DFT-spread OFDM \((N=M)\). It should be noted that \( N=M=12 \) has been verified as the optimal gap width with a bias current of 80 mA in this work.

Since the matrix \( W \) and \( W^H \) are no longer orthogonal, the ICI is purposely induced in the proposed scheme. The cascaded binary-phase-shift-keying iterative detection (CBID) [16] is an effective algorithm to mitigate the ICI based on the \( N \times N \) correlation matrix \( C=W^H W \), where the \((i, k)\)-th entry of \( C \) is given by

\[
C_{ik} = \sum_{m=0}^{M-1} \exp(-j2\pi m(k-i)/N)/M.
\]

In the \( g \)-th iteration of CBID, the received symbols \( \tilde{S}_g \) after the INODFT matrix decoding is first updated by

\[
\tilde{S}_g = R + (I - C)\tilde{S}_{g-1},
\]

where \( R \) is the decoded symbols after the INODFT matrix, \( I \) is the identity matrix, and \( \tilde{S}_{g-1} \) is the symbols after the \((g-1)\)-th iteration. As depicted in Fig. 2(b), the symbols inside areas A and B after the above iterations are mapped onto the corresponding constellation points, leaving other symbols unchanged until the next iteration. The threshold interval during the iteration is updated by \( \Delta t=1-g/G \), where \( G \) is the preset total number of iterations.

The VNLE is also considered a useful nonlinear distortion compensation scheme. The output of the time domain \( \nu \)-th order VNLE can be expressed as [17],

\[
j[l] = \sum_{l=-1}^{L-1} h_l(l) x(t-l) + \sum_{l=0}^{L-1} \sum_{l_1=0}^{l} h_2(l_1, l_2) 2 \sum_{\mu=1}^{l} x(t-l_\mu) + \cdots
+ \sum_{l=0}^{L-1} \sum_{l_1=0}^{l} \cdots \sum_{l_{v-1}=0}^{l} h_v(l_1, l_2, \ldots, l_v) \prod_{\mu=1}^{v-1} x(t-l_\mu),
\]

where \( x[t-l] \) is the \((t-l)\)-th sample of the received signal, \( y[t] \) is the \( t \)-th sample of the output signal after VNLE, \( h_1(l_1, l_2, \ldots, l_v) \) is the weighting coefficient of the \( \nu \)-th order which is obtained by the \( \nu/2 \)-spaced RLS algorithm in this work, \( L_1 \) is the memory length of the \( \nu \)-th order kernel. As the nonlinear distortion in this work is mainly of the second-order, only the diagonal terms of the third-order kernel are included in the third-order filtering to reduce the complexity, i.e., \( l_i=l_j=l_k \) for the third-order kernels.

Then, we compared the computational complexity of the proposed NODFT-p gapped-OFDM with the \( \nu/2 \)-spaced RLS-based third-order VNLE. For a fair comparison, we also consider the complexity required for updating the coefficients of the VNLE, i.e., the complexity of the time-domain \( \nu/2 \)-spaced RLS algorithm, and the complexity of the frequency-domain zeros-forcing (ZF) equalizer. The RLS algorithm recursively finds the coefficients of the VNLE [18] in the training process at the receiver side, and this iterative process usually requires multiple iterations, i.e., \((N_M+N_p)\) iterations required for each training OFDM symbol in this Letter, where \( N_p \) is the size of IDFT used at the transmitter side to produce...
the real-valued signal, and $N_n$ is the length of cyclic prefix (CP) to combat CD. Based on [18], the required numbers of multiplications and additions for the time-domain $T/2$-spaced RLS algorithm in one iteration are $3L^2+2L(L+L_n+L) + 4L_{n}+1$, and $2L^2+L_{n}+1$, respectively, where $L=L_n+L_n(L+1)/2+L_0$ is the total tap number of the used third-order VNLE. As shown in ref [17], the corresponding input-output relationship of the VNLE can be expressed in the form of vector multiplication. Then, the required numbers of multiplications and additions for the third-order VNLE when equalizing one OFDM symbol are $(N_n+N_s)(L+L_n(L+1)+4L_n)$, and $(N_n+N_s)(L-1)$, respectively. The ZF equalizer is a simple single-tap equalizer [19]. It does not need additions, but needs $M$ multiplications for finding channel coefficients or equalizing one OFDM symbol. The details of the CBID algorithm can be found in [16], and based on [16], the required numbers of multiplications and additions for the CBID algorithm when decoding one OFDM symbol are $4GN^2+MN$ and $3GN+7GN+(M-1)N$, respectively. Since both the proposed NODFT-p gapped-OFDM and the $T/2$-spaced RLS-based third-order VNLE require the fast Fourier transform (FFT) algorithm at the receiver side to transform the time-domain signal into frequency-domain, we ignore the complexity induced by this operation. Table 1 summarizes the required computational complexity of these two schemes.

We finally experimentally investigated the performance of the proposed scheme. Fig. 3 shows the experimental setup and the digital signal processing (DSP). At the transmitter, the bit-stream after serial-to-parallel conversion (S/P) was first mapped onto QAM-4 symbols, which were allocated over 230 subcarriers ($N=230$), and then transformed into $M$ subcarriers by the NODFT matrix. Hermitean symmetry was applied before performing a 512-point inverse fast Fourier transform (IFFT) to generate a real-valued signal. Then, a CP with a length of 16 was added to combat CD. To estimate the channel response and implement equalization at the receiver, 30 blocks of QAM-4 training sequences (TS) were added before the 300 blocks of OFDM payload symbols. A 12-Gsa/s arbitrary waveform generator (AWG) together with a DML at a center wavelength of 1546.2 nm converted the signal from the digital domain to the optical domain, where the threshold current of the DML was 11.2 mA. Therefore, the data rate of the signal was 9.5 Gb/s (≈ 12G × 2 bits × 230/512 × 512/528 × 300/330). After 100-km SSMF transmission, an optical bandpass filter (OBPF) was employed after the output of the second erbium-doped fiber amplifier (EDFA) to suppress the out-of-band amplified spontaneous emission noise. A variable optical attenuator (VOA) was used to vary received optical power (ROP) to evaluate the sensitivity curve. The signal was then detected by a 40-GHz photodiode (PD) and finally captured by a real-time oscilloscope operating at 80 Gsa/s for offline DSP. It should be noted that the inherent driver of DML is AC-coupled and the cut-off frequency of the bias-tee is 10 MHz, which is comparable with the subcarrier spacing (6 GHz/230 ≈ 26.1 MHz), to reduce its influence on low-frequency subcarriers and keep the SE unchanged, we shifted 2 mo-

*Table 1. Computational Complexity of Different Compensation Algorithm for One OFDM Symbol*

<table>
<thead>
<tr>
<th>Multiplications/Symbol</th>
<th>Additions/Symbol</th>
</tr>
</thead>
<tbody>
<tr>
<td>(3$L^2$+2L$L_n$+L$+\bar{L}_n$+1)+4$L_n$+1)</td>
<td>(3$N_n$+2$L_n$)(L+1)+4$L_n$+1)</td>
</tr>
<tr>
<td>(N_n+N_s)(L$+\bar{L}_n$+1)+4$L_n$+1)</td>
<td>(N_n+N_s)(L+1)+4$L_n$+1)</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>RLS</th>
<th>Third-order VNLE</th>
<th>ZF equalizer</th>
<th>CBID algorithm</th>
</tr>
</thead>
<tbody>
<tr>
<td>$3L^2+2L(L+L_n+L) + 4L_n+1$</td>
<td>$(N_n+N_s)(L+L_n(L+1)+4L_n)$</td>
<td>$M$</td>
<td>$4GN^2+MN$</td>
</tr>
<tr>
<td>$2L^2+L_n+1$</td>
<td>$(N_n+N_s)(L-1)$</td>
<td>0</td>
<td>$3GN+7GN+(M-1)N$</td>
</tr>
</tbody>
</table>

*Fig. 3 Experimental setup and DSP of the proposed NODFT-p gapped-OFDM. (AWG: arbitrary waveform generator, EA: electrical amplifier, VOA: variable optical attenuator, PD: photodiode, DSO: digital oscilloscope. Inset (i): Measured optical spectra under different modulation cases at BTB. (b) BER performance as a function of (a) driving voltage Vpp, where the bias current was set to 80 mA; and (b) bias current, where Vpp was set to the corresponding optimum value.*
mainly falls within the low-frequency band, and the gapped OFDM makes it possible to avoid much of the distortion [11]. Besides, abandoning these subcarriers located at the low-frequency band with low SNR is also helpful in alleviating the impairment. However, the ICI induced by the non-orthogonal precoding and decoding increases as the gap width increases [15], and it may also result in the loss of the subcarriers with high SNR if the gap width is too large. Therefore, an optimal gap width exists to fully utilize the subcarriers that are suitable for data transmission.

Fig. 5(b) depicts the impact of the gap width on the bit-error rate (BER) performance, the BER first decreases along with the growing gap width, thanks to the abandonment of the subcarriers with low SNR due to nonlinear distortion. The BER then increases with the growing gap width because of the increased ICI and the sacrifice of subcarriers with high SNR. The optimal gap width is obtained at \( N-M=12 \), corresponding to a \( \approx 0.28 \)-GHz bandwidth. And the corresponding optimal number of iterations \( G \) in CBID was set to 4.

Fig. 6(a) shows the measured ROP sensitivity of the received signals. Herein, we have also studied the performance of shifting the modulated subcarriers directly to high frequency by the optimized gap width \( (N-M) \) for comparison. The optimal tap number of the \( T/2 \) RLS-based third-order VNLE was \((91, 16, 7)\). As shown in Fig. 6(a), for the case of 100-km SSMF transmission where there is higher nonlinear distortion generated by the interaction between chirp and CD, the DCO-OFDM with shifting using VNLE performs best since it can avoid much nonlinear distortion distributed in low-frequency and eliminate the residual nonlinearity with the powerful VNLE. However, it should be noted that subcarrier shifting is not universally applicable considering the bandwidth limitation and the case when \( N \) is close to \( N_g/2 \). Besides, the proposed scheme achieved \( \approx 0.4\)-dB sensitivity improvement at the KP4-FEC threshold over the conventional DCO-OFDM using VNLE. Based on the computational complexity analysis summarized in Table 1, the proposed scheme with the optimal gap width can reduce the computational complexity by 90% for multiplication, and 88.32% for addition, respectively, compared to the schemes using VNLE. For the BTB case, we can see that the proposed scheme with a gap at low frequency shows worse performance than that after SSMF transmission. This can be explained by the Inset (i) of Fig. 6, where the B2B SNR has a frequency roll-off but the performance of its high-frequency part is enhanced after SSMF transmission due to the interaction between chirp and CD [6]. That is why setting a gap at the low frequency only works in the 100-km case. Fig. 6(b) presents the measured SNR curves of different schemes, indicating that the NODFT-p can spread the noise evenly over subcarriers and CBID can further improve the overall SNR.

In this Letter, we have proposed an NODFT-p gapped-OFDM scheme to mitigate the nonlinear distortion in a DML-based optical transmission system. Different from the conventional gapped-OFDM, the proposed scheme can reduce the nonlinear distortion without sacrificing the SE. The performance improvement and the computational complexity reduction of the proposed scheme have been experimentally verified when compared with the conventional VNLE scheme, both at the optimal setting. In conclusion, the proposed scheme is a promising technique to eliminate the nonlinear distortion in a DML-based system.

**Disclosures.** The authors declare no conflicts of interest.

**Data availability.** Data underlying the results presented in this paper are not publicly available at this time but may be obtained from the authors upon reasonable request.

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